A1\_Problem1

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library("gurobi")

## Loading required package: slam

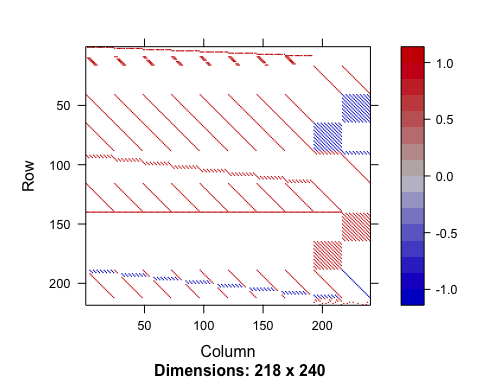
library("Matrix")  
library("igraph")

##   
## Attaching package: 'igraph'

## The following objects are masked from 'package:stats':  
##   
## decompose, spectrum

## The following object is masked from 'package:base':  
##   
## union

library("rdist")  
  
n <- 8  
k <- 3  
  
M <- 100000  
T.ij = matrix(c(M, M, 60, 90, M, 180, M, M, M, M, 30, 60, M, 150, M, M, M, M, M, M, 30, M, 90, M, M, M, M, M, M, M, 30, M, M, M, M, M, M, 30, M, M, M, M, M, M, M, M, M, 90, M, M, M, M, M, M, M, 60, M, M, M, M, M, M, M, M), nrow = n, ncol=n, byrow = TRUE)  
F.ik.S.ik = c(rep(0, n\*k\*2))  
cvec = c(rep(0, n\*n\*k),F.ik.S.ik)  
col = 1  
for(i in 1:n){  
 for(j in 1:n){  
 for(K in 1:k){  
 cvec[col] = T.ij[i,j]  
 col = col + 1  
 }  
 }  
}  
  
bvec = c(rep(1, n), rep(1, n), rep(1, n\*k), rep(0, n\*k), rep(0, n\*k), rep(0, k), rep(1, n\*k), rep(1, n\*k), 8, rep(1, n\*k), rep(1, n\*k), rep(0, n\*k), rep(0, 6) )  
dir = c(rep("<=", n), rep("<=", n), rep("<=", n\*k), rep(">=", n\*k), rep(">=", n\*k), rep("=", k), rep("<=", n\*k), rep("<=", n\*k), "=", rep("<=", n\*k), rep("<=", n\*k), rep("=", n\*k), rep("=", 6))  
  
Amat = matrix(0, nrow=(n\*2+(n\*k)\*8+k+7), ncol=(n\*n\*k + n\*k\*2))  
#contraint 1  
for (i in 1:n) {  
 Amat[i, ((i - 1) \* n\*k + 1):(i \* n\*k)] = 1  
 Amat[i, ((i - 1) \* n\*k + i)] = 0  
 Amat[i, ((i - 1) \* n\*k + i + n)] = 0  
 Amat[i, ((i - 1) \* n\*k + i + n\*2)] = 0  
}  
#contraint 2  
for (i in 1:n) {  
 Amat[i+n, seq(i,by =n\*k, length.out = n)] = 1  
 Amat[i+n, seq(i+1,by =n\*k, length.out = n)] = 1  
 Amat[i+n, seq(i+2,by =n\*k, length.out = n)] = 1  
 Amat[i+n, ((i - 1) \* n\*k + 1):(i \* n\*k)] = 0  
}  
#contraint 3  
row = 1  
for (i in 1:n) {  
 for(K in 1:k){  
 Amat[row+n\*2, seq(from=row+n\*n\*k,by =n\*k, length.out = 2)] = 1  
 row = row + 1  
 }  
}  
#contraint 4  
row = 1  
col = 1  
for (i in 1:n) {  
 for(K in 1:k){  
 Amat[row+n\*2+n\*k, seq(row,by =n\*k, length.out = n)] = 1  
 Amat[row+n\*2+n\*k, seq(from=n\*n\*k+n\*k+col,by =k, length.out = n)] = -1  
 row = row + 1  
 col = col + 1  
 }  
 col = 1  
}  
#contraint 5  
row = 1  
col = 1  
for (i in 1:n) {  
 for(K in 1:k){  
 Amat[row+n\*2+n\*k\*2, seq(row,by =n\*k, length.out = n)] = 1  
 Amat[row+n\*2+n\*k\*2, seq(from=n\*n\*k+col,by =k, length.out = n)] = -1  
 row = row + 1  
 col = col + 1  
 }  
 col = 1  
}  
#contraint 6  
for (i in 1:(k)) {  
 Amat[i+n\*2+n\*k\*3, seq(from=n\*n\*k+i,by =k, length.out = n)] = 1  
 Amat[i+n\*2+n\*k\*3, seq(from=n\*n\*k+n\*k+i,by =k, length.out = n)] = -1  
}  
  
#contraint 7  
Count = 1  
Count2 = 1  
for(i in 1:n){  
 for(K in 1:k){  
 Amat[Count+n\*2+n\*k\*3+k,seq(from=Count2,by =k, length.out = n)] = 1  
 Amat[Count+n\*2+n\*k\*3+k,216+Count] = 1  
 Count = Count + 1  
 Count2 = Count2 + 1  
 }  
 Count2 = Count2 + (n-1)\*k  
}  
  
#contraint 8  
Count = 1  
Count2 = 1  
for(i in 1:n){  
 for(K in 1:k){  
 Amat[Count+n\*2+n\*k\*4+k,seq(from=Count2,by =n\*k, length.out = n)] = 1  
 Amat[Count+n\*2+n\*k\*4+k,192+Count] = 1  
 Count = Count + 1  
 Count2 = Count2 + 1  
 }  
 #Count2 = Count2 + (n-1)\*k  
}  
  
#Constraint 9: make sure that when you sum all F and all X it equals to 8  
Amat[n\*2+n\*k\*5+k+1,(1):(n\*n\*k + n\*k)] = 1  
  
#Constraint 10: each crew can only have first flight once  
row = 1  
col = 1  
for (i in 1:n) {  
 for(K in 1:k){  
 Amat[row+n\*2+n\*k\*5+k+1, seq(from=n\*n\*k+n\*k+col,by =k, length.out = n)] = 1  
 row = row + 1  
 col = col + 1  
 }  
 col = 1  
}  
#Constraint 11: each crew can only have last flight once  
row = 1  
col = 1  
for (i in 1:n) {  
 for(K in 1:k){  
 Amat[row+n\*2+n\*k\*6+k+1, seq(from=n\*n\*k+col,by =k, length.out = n)] = 1  
 row = row + 1  
 col = col + 1  
 }  
 col = 1  
}  
#Constraint 12: make sure that if a crew goes from i to j then j to something else should still be done by the same crew (His paper)  
row = 1  
offSet = 0  
offSet2 = 0  
for (i in 1:n) {  
 for(K in 1:k){  
 Amat[row+n\*2+n\*k\*7+k+1, seq(row,by =n\*k, length.out = n)] = 1  
 Amat[row+n\*2+n\*k\*7+k+1, seq(K + offSet2,by =n\*k, length.out = 1)] = 0  
 Amat[row+n\*2+n\*k\*7+k+1, seq(row + offSet + k,by =k, length.out = n-1)] = -1  
 Amat[row+n\*2+n\*k\*7+k+1, seq(from=row+n\*n\*k,by =n\*k, length.out = 1)] = 1  
 Amat[row+n\*2+n\*k\*7+k+1, seq(from=row+n\*n\*k+n\*k,by =n\*k, length.out = 1)] = -1  
 row = row + 1  
 }  
 offSet = offSet + 24  
 offSet2 = offSet2 + 27  
}  
  
#constraint 13: make sure that if someone starts somewhere it also needs to end in the same city  
Crew1NotF = c(2,3,4,6,8)  
for(i in 1:length(Crew1NotF)){  
 Amat[n\*2+n\*k\*8+k+2, n\*n\*k+(Crew1NotF[i]-1)\*3+1] = 1  
}  
Crew2NotF = c(1,2,5,7,8)  
for(i in 1:length(Crew2NotF)){  
 Amat[n\*2+n\*k\*8+k+3, n\*n\*k+(Crew2NotF[i]-1)\*3+2] = 1  
}  
Crew3NotF = c(1,2,5,7,8)  
for(i in 1:length(Crew3NotF)){  
 Amat[n\*2+n\*k\*8+k+4, n\*n\*k+(Crew3NotF[i]-1)\*3+3] = 1  
}  
  
#Constraint 14: make sure that each crew can only start in one given city  
Crew1F = c(1,5,7)  
for(i in 1:length(Crew1F)){  
 Amat[n\*2+n\*k\*8+k+5, n\*n\*k+(Crew1F[i]-1)\*3+1] = 1  
}  
Crew1L = c(3,4,8)  
for(i in 1:length(Crew1L)){  
 Amat[n\*2+n\*k\*8+k+5, n\*n\*k+n\*k+(Crew1L[i]-1)\*3+1] = 1  
}  
Crew2F = c(3,4,6)  
for(i in 1:length(Crew2F)){  
 Amat[n\*2+n\*k\*8+k+6, n\*n\*k+(Crew2F[i]-1)\*3+2] = 1  
}  
Crew2L = c(1,2,5)  
for(i in 1:length(Crew2L)){  
 Amat[n\*2+n\*k\*8+k+6, n\*n\*k+n\*k+(Crew2L[i]-1)\*3+2] = 1  
}  
Crew3F = c(2,8)  
for(i in 1:length(Crew3F)){  
 Amat[n\*2+n\*k\*8+k+7, n\*n\*k+(Crew3F[i]-1)\*3+3] = 1  
}  
Crew3L = c(6,7)  
for(i in 1:length(Crew3L)){  
 Amat[n\*2+n\*k\*8+k+7, n\*n\*k+n\*k+(Crew3L[i]-1)\*3+3] = 1  
}  
  
  
image(Matrix(Amat))



myLP = list()  
myLP$obj = cvec  
myLP$A = Amat  
myLP$sense = dir  
myLP$rhs = bvec  
myLP$vtypes = "B"  
myLP$ub = 1  
  
mysol = gurobi(myLP)

## Warning for adding variables: zero or small (< 1e-13) coefficients, ignored  
## Optimize a model with 218 rows, 240 columns and 2647 nonzeros  
## Variable types: 0 continuous, 240 integer (240 binary)  
## Coefficient statistics:  
## Matrix range [1e+00, 1e+00]  
## Objective range [3e+01, 1e+05]  
## Bounds range [1e+00, 1e+00]  
## RHS range [1e+00, 8e+00]  
## Found heuristic solution: objective 800000.00000  
## Presolve removed 137 rows and 72 columns  
## Presolve time: 0.02s  
## Presolved: 81 rows, 168 columns, 1180 nonzeros  
## Variable types: 0 continuous, 168 integer (168 binary)  
##   
## Root relaxation: objective 2.502400e+05, 55 iterations, 0.00 seconds  
##   
## Nodes | Current Node | Objective Bounds | Work  
## Expl Unexpl | Obj Depth IntInf | Incumbent BestBd Gap | It/Node Time  
##   
## 0 0 250240.000 0 6 800000.000 250240.000 68.7% - 0s  
## H 0 0 400180.00000 250240.000 37.5% - 0s  
## 0 0 250240.000 0 12 400180.000 250240.000 37.5% - 0s  
## H 0 0 400150.00000 250240.000 37.5% - 0s  
## \* 0 0 0 300180.00000 300180.000 0.00% - 0s  
##   
## Cutting planes:  
## Gomory: 2  
##   
## Explored 1 nodes (88 simplex iterations) in 0.04 seconds  
## Thread count was 4 (of 4 available processors)  
##   
## Solution count 4: 300180 400150 400180 800000   
##   
## Optimal solution found (tolerance 1.00e-04)  
## Best objective 3.001800000000e+05, best bound 3.001800000000e+05, gap 0.0000%

mysol$objval

## [1] 300180

mysol$x

## [1] 0 0 0 0 0 0 0 0 0 0 0 0 0 0 0 0 0 0 0 0 0 0 0 0 0 0 0 0 0 0 0 0 0 0 1  
## [36] 0 0 0 0 0 0 0 0 0 0 0 0 0 0 0 0 0 0 0 0 0 0 0 0 0 0 1 0 0 0 0 0 0 0 0  
## [71] 0 0 0 0 0 0 0 0 0 0 0 0 0 0 0 0 0 0 0 0 1 1 0 0 0 0 0 0 0 0 0 0 0 0 0  
## [106] 0 0 0 0 0 0 0 1 0 0 0 0 0 0 0 0 0 0 0 0 0 0 0 0 0 0 0 0 0 0 0 0 0 0 0  
## [141] 0 0 0 0 0 0 0 0 1 0 0 0 0 0 0 0 0 0 0 0 0 0 0 0 0 0 0 0 0 0 0 0 0 0 0  
## [176] 1 0 1 0 0 0 0 0 0 0 0 0 0 0 0 0 0 0 0 0 0 0 0 0 0 0 0 0 0 0 0 0 0 0 0  
## [211] 0 0 0 0 0 0 0 0 0 0 0 0 0 0 0 0 0 0 0 0 0 0 0 0 0 0 0 0 0 0